

**Classical limit** At low frequencies, the spectral intensity is given by

$$S_{\omega}(\omega) \approx \frac{\omega^2 k_B T}{4\pi^3 c^2} \quad \text{where } \hbar\omega \ll k_B T \quad (1)$$

Draw a graph with the classical limit of  $S_{\omega}$  on the vertical axis, and the frequency  $\omega$  (or alternatively  $\hbar\omega$ ) on the horizontal axis. Sketch this relationship for the two temperatures  $T = 300$  K and  $T = 600$  K.

**High-frequency quantum limit** At high frequencies, when the energy quanta are much greater than  $k_B T$ , the spectral intensity becomes

$$S_{\omega}(\omega) \approx \frac{\hbar\omega^3}{4\pi^3 c^2} e^{-\frac{\hbar\omega}{k_B T}} \quad \text{where } \hbar\omega \gg k_B T \quad (2)$$

**On the same graph** sketch use this high frequency limit to sketch the spectral distribution over the entire frequency range at the same two temperatures.

**Find the total** Using your graphs, try to estimate the ratio between the **intensity** at the two temperatures. Keep in mind that the **intensity** is the integral of the **spectral intensity** over all possible frequencies.

When we double the temperature does the intensity

1. Increase by 2 times
2. Increase by 4 times
3. Increase by 8 times
4. Increase by 16 times