

1 Find Area/Volume from the Vector Differential

Start with $d\vec{r}$ in rectangular, cylindrical, and spherical coordinates. Use these expressions to write the scalar area elements dA (for different coordinate equals constant surfaces) and the volume element $d\tau$. It might help you to think of the following surfaces: The various sides of a rectangular box, a finite cylinder with a top and a bottom, a half cylinder, and a hemisphere with both a curved and a flat side, and a cone.

(a) Rectangular:

$$dA = \quad (1)$$

$$d\tau = \quad (2)$$

(b) Cylindrical:

$$dA = \quad (3)$$

$$d\tau = \quad (4)$$

(c) Spherical:

$$dA = \quad (5)$$

$$d\tau = \quad (6)$$

2 Flux through a Cylinder

- (a) What do you think will be the flux through the cylindrical surface that is placed as shown in the constant vector field in the first figure?
- (b) What if the cylinder is placed upright, as shown in the second figure? Explain.

